

$$\begin{array}{ccc}
 \{1\} \times \mathrm{Map}_{\mathcal{C}_{\mathfrak{m}}}(X \otimes M, N) & \hookrightarrow & \mathcal{C}_{\mathfrak{a}} \times_{\mathcal{C}_{\mathfrak{m}}} \mathcal{C}_{\mathfrak{m}/N} \\
 \downarrow & \nearrow \text{dashed} & \downarrow f \\
 \Delta^1 \times \mathrm{Map}_{\mathcal{C}_{\mathfrak{m}}}(X \otimes M, N) & & \mathcal{C}_{\mathfrak{a}} \\
 & \searrow & \nearrow e \\
 & \Delta^1 &
 \end{array}$$